Modelling gas and dust during star formation

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ALMA images of discs in nearby star forming regions



DSHARP ALMA Large Program; Andrews et al. 2018

ALMA images of Class 0 multiple systems



VANDAM Survey; Tobin et al. 2018





- Two methods for modelling drag force between gas and dust with SPH:
 - Two-fluid method (Laibe & Price 2012; Ayliffe et al. 2012; Loren-Aguilar & Bate 2014)
 - One-fluid method (Laibe & Price 2014a,b; Price & Laibe 2015)
- One-fluid method cannot handle large grains
- Two-fluid prone to artificial clumping and resolution-dependent over-dissipation

Two-fluid equations

One-fluid equations

$$\begin{split} \frac{\partial \hat{\rho}_{g}}{\partial t} + \nabla .\left(\hat{\rho}_{g}\boldsymbol{v}_{g}\right) &= 0, \\ \frac{\partial \hat{\rho}_{d}}{\partial t} + \nabla .\left(\hat{\rho}_{d}\boldsymbol{v}_{d}\right) &= 0, \\ \hat{\rho}_{g}\left(\frac{\partial \boldsymbol{v}_{g}}{\partial t} + \boldsymbol{v}_{g}.\nabla \boldsymbol{v}_{g}\right) &= -\theta \ \nabla P_{g} + \hat{\rho}_{g}\boldsymbol{f} - \boldsymbol{F}_{drag}^{V}, \\ \hat{\rho}_{d}\left(\frac{\partial \boldsymbol{v}_{d}}{\partial t} + \boldsymbol{v}_{d}.\nabla \boldsymbol{v}_{d}\right) &= -\nabla P_{d} - (1-\theta) \ \nabla P_{g} + \hat{\rho}_{d}\boldsymbol{f} + \boldsymbol{F}_{drag}^{V}, \\ \boldsymbol{F}_{drag}^{V} &= K(\boldsymbol{v}_{g} - \boldsymbol{v}_{d}). \end{split}$$

$$\begin{split} \frac{\mathrm{d}\rho}{\mathrm{d}t} &= -\rho(\nabla \cdot \boldsymbol{v}), \\ \frac{\mathrm{d}\boldsymbol{v}}{\mathrm{d}t} &= -\frac{\nabla P_{\mathrm{g}}}{\rho}, \qquad \boldsymbol{v} = \frac{\rho_{\mathrm{g}}\boldsymbol{v}_{\mathrm{g}} + \rho_{\mathrm{d}}\boldsymbol{v}_{\mathrm{d}}}{\rho_{\mathrm{g}} + \rho_{\mathrm{d}}} \\ \frac{\mathrm{d}\epsilon}{\mathrm{d}t} &= -\frac{1}{\rho}\nabla \cdot (\epsilon t_{\mathrm{s}} \nabla P_{\mathrm{g}}), \\ P &= c_{\mathrm{s}}^{2}\rho_{\mathrm{g}} = c_{\mathrm{s}}^{2}(1 - \epsilon)\rho, \end{split}$$





Dust dynamics in molecular clouds

• Small dust particles (~0.1µm) are collisionally coupled to gas

- Usually assume that dust and gas are well mixed in molecular clouds
- Gas to dust ratio ~100
- But large dust particles may be poorly coupled
- May be a population of large grains (>1 μ m) in molecular clouds
 - Cloud-shine observations (e.g. Foster & Goodman 2006; Steinacker et al. 2014, 2015)
 - Mid-IR extinction (e.g. Wang, Li & Jiang 2015a,b) and sub-mm emissivity (e.g. Miettinen et al. 2012; Schnee et al. 2014)



Dust dynamics in molecular clouds

- Dust dynamics depend on grain size
 - Small grains (~0.1 micron) are well-coupled to the gas
 - Dust-to-gas ratio of larger grains can vary
 - Leads to size-sorting in molecular clouds









Dust dynamics during protostellar collapse

- In Exeter, we've been starting to study smaller scales
- Using two-fluid dust-gas SPH simulations
- Studying dynamics of different grain sizes during protostellar collapse
 - Used two-fluid gas/dust SPH simulations (Bate & Loren-Aguilar 2017)
 - Rotating Bonnor-Ebert spheres, dust initially well-mixed and moving with gas





Rapidly-rotating molecular cloud core



Bate & Loren-Aguilar (2017)





Slowly-rotating molecular cloud core



Bate & Loren-Aguilar (2017)





Dust dynamics during protostellar collapse

- Large grains (size >10μm) collapse faster than gas
 - Experience gravity, but not gas pressure

Implications if large grains are present

- Dust-to-gas ratio (of large grains) may increase in central regions
- Produces a size-distribution favouring large grains without grain growth (size sorting)
- Large grains pass through the midplane, oscillate, and settle to disc-like geometry *before* gas has collapsed to form a protostar





Dust dynamics during disc formation

- Potential numerical issues
 - Self-gravity can exacerbate clumping of dust particles
 - Produce local gravitational collapse
- Use sink particles to follow collapse beyond first hydrostatic core phase
- Initial conditions
 - Unstable Bonnor-Ebert sphere
 - Solid body rotation + turbulent velocity field
 - Dust-to-gas ratio initially uniform



Dust in a turbulent, collapsing molecular cloud core

100 µm Dust

1 mm Dust

DiRAC

erc



Bate, in preparation





Dust dynamics during disc formation

• Grains with sizes <100µm are well-coupled to the gas

- Larger grains, if present
 - Tend to enhance structures (e.g. spiral arms and filaments)
 - Rapidly undergo radial migration mm dust disc smaller than gas disc

• Future work

• Need to begin with small grains and treat dust growth